

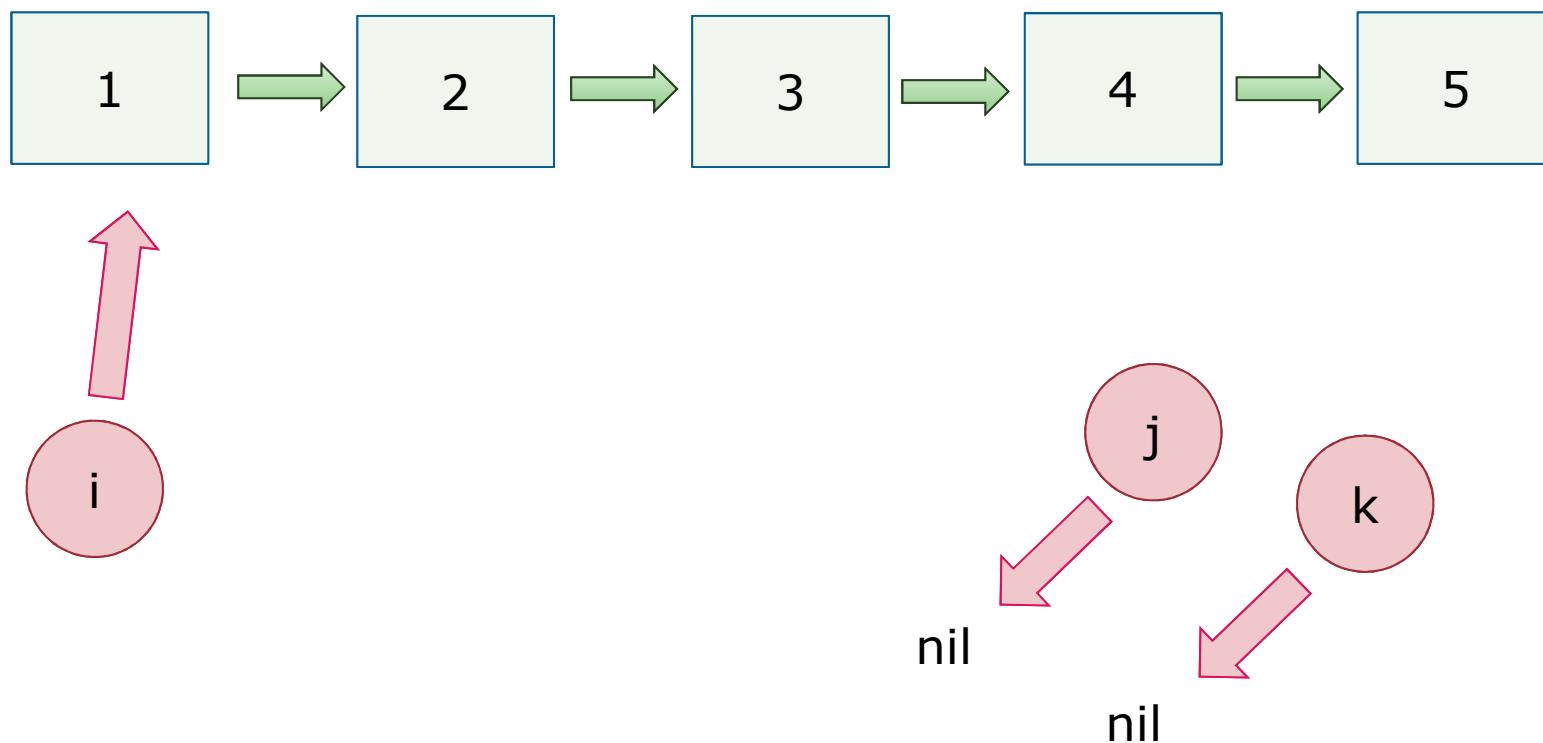
Separation as Abstraction

Nisansala Yatapanage
with Cliff Jones and Andrius Velykis
Newcastle University

- Issues of separation are well handled by Concurrent Separation Logic.
- (at least) Some examples can be clearly developed using layers of abstraction.
- Two examples: Reynolds' in-place list reversal algorithm and concurrent DOM trees.

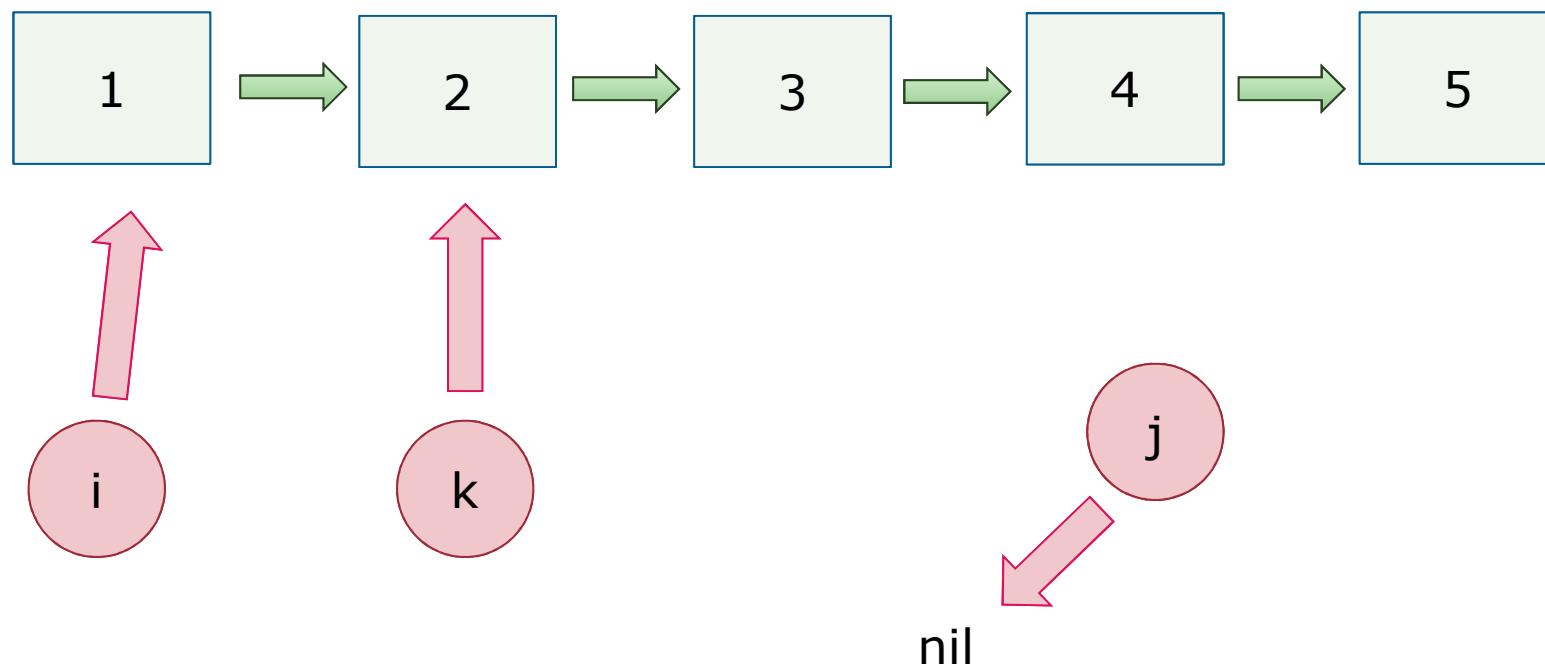
In-place List Reversal

Originally presented by John Reynolds



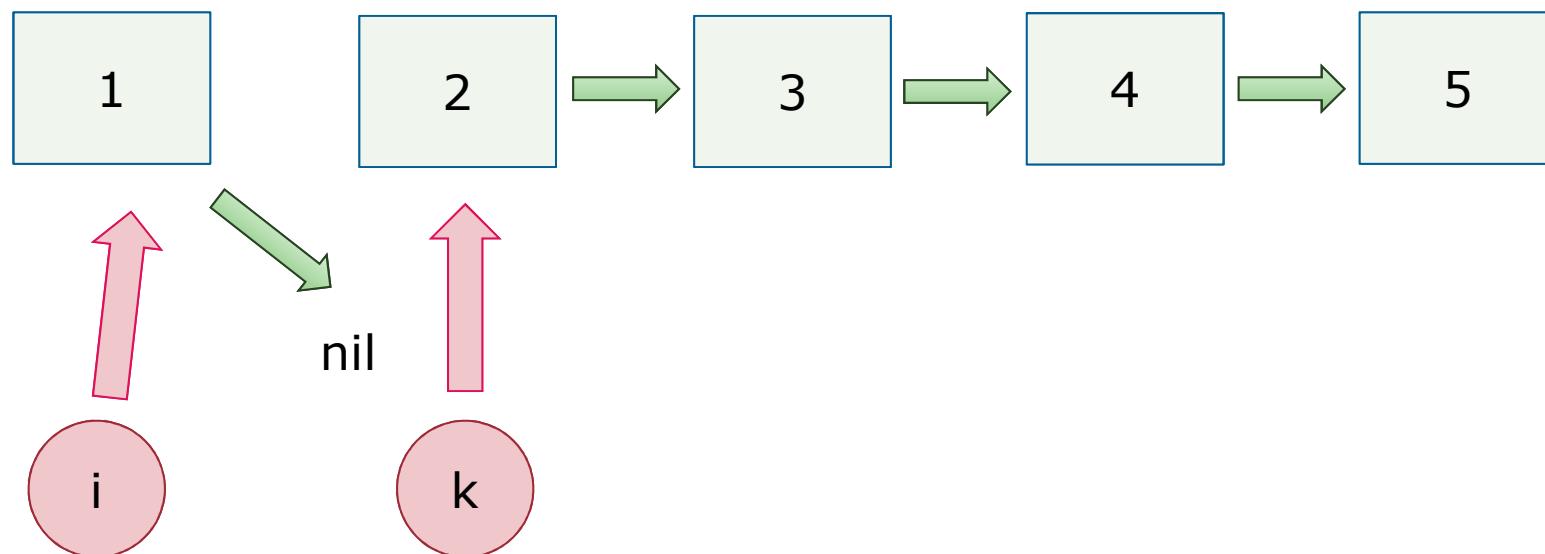
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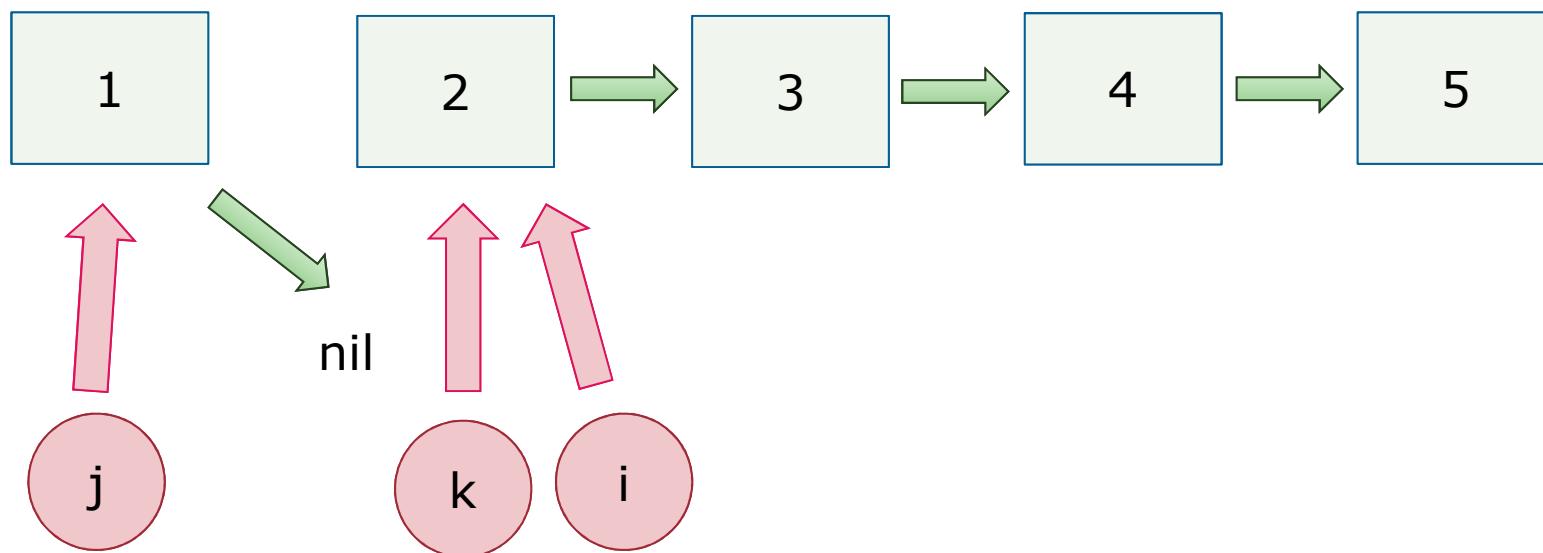
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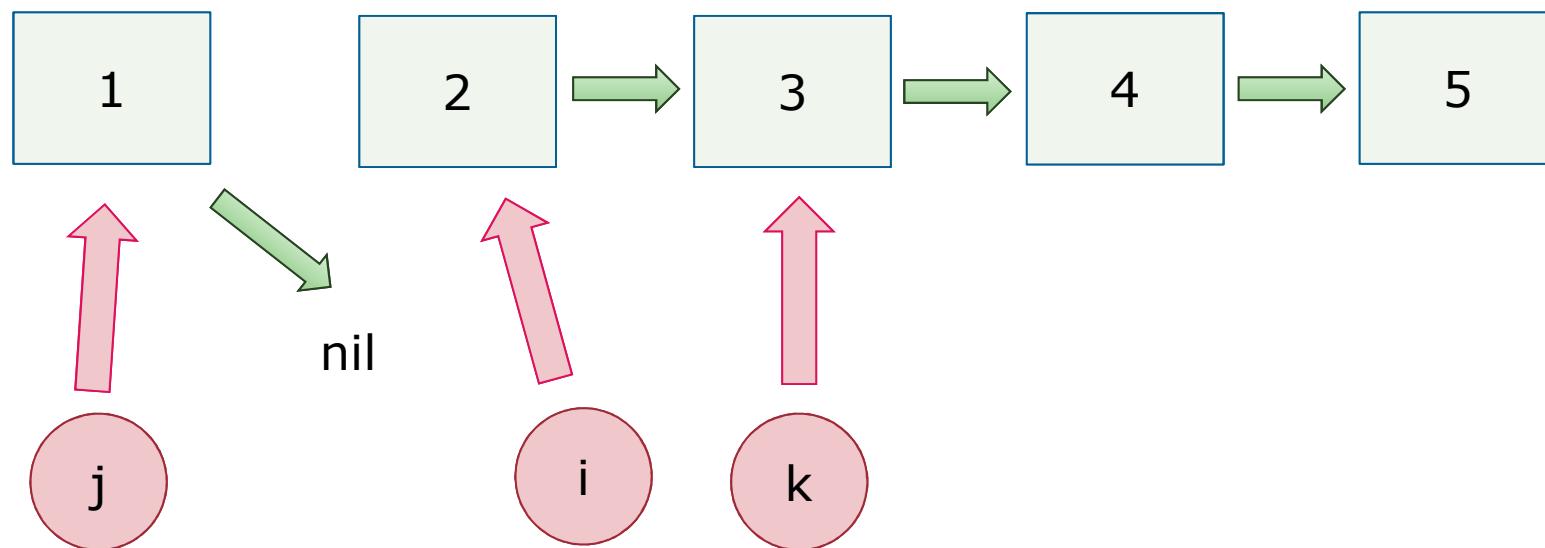
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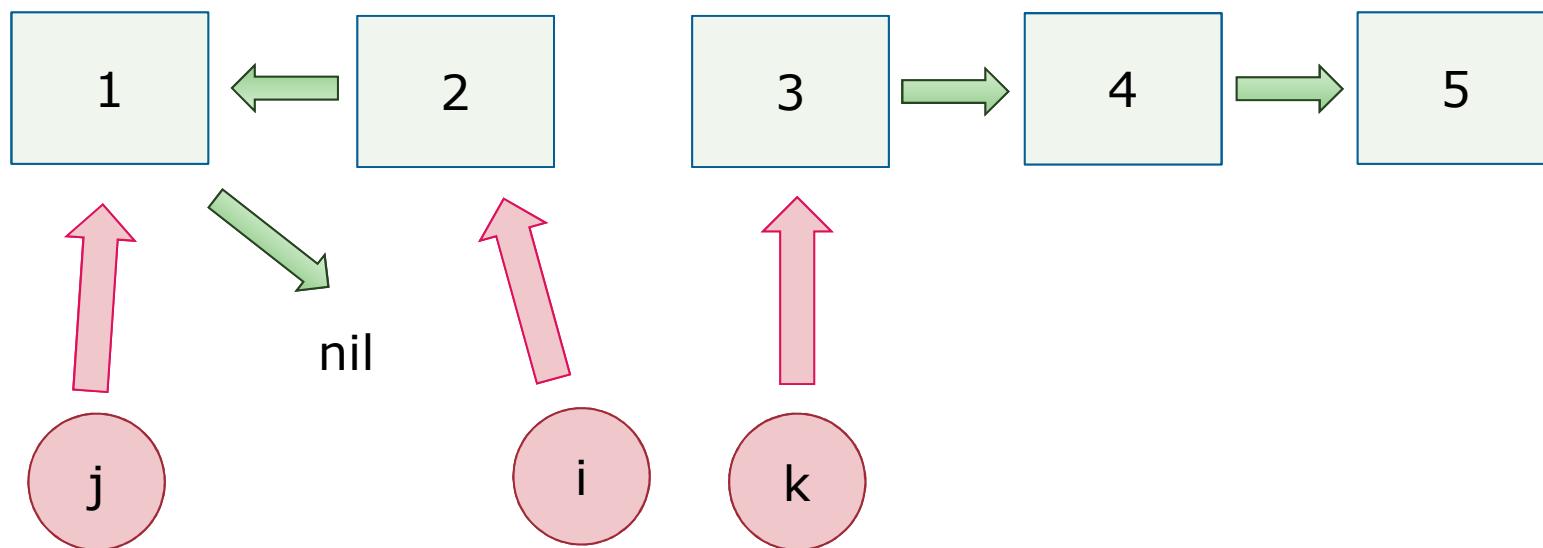
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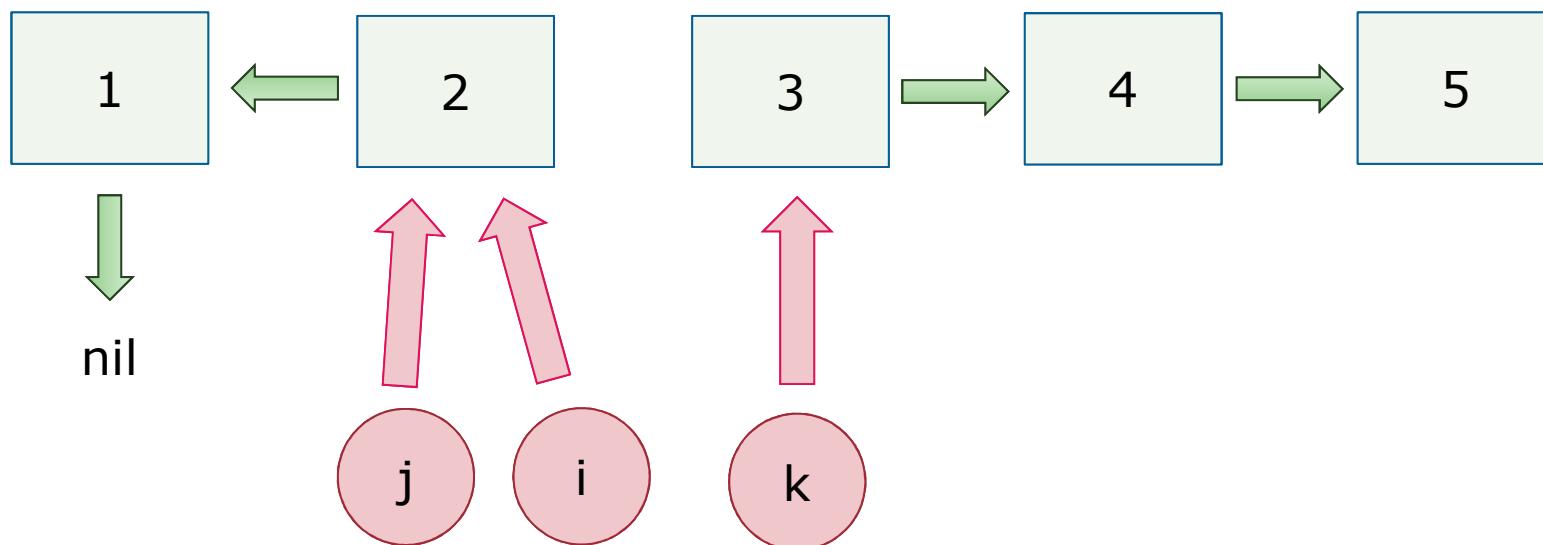
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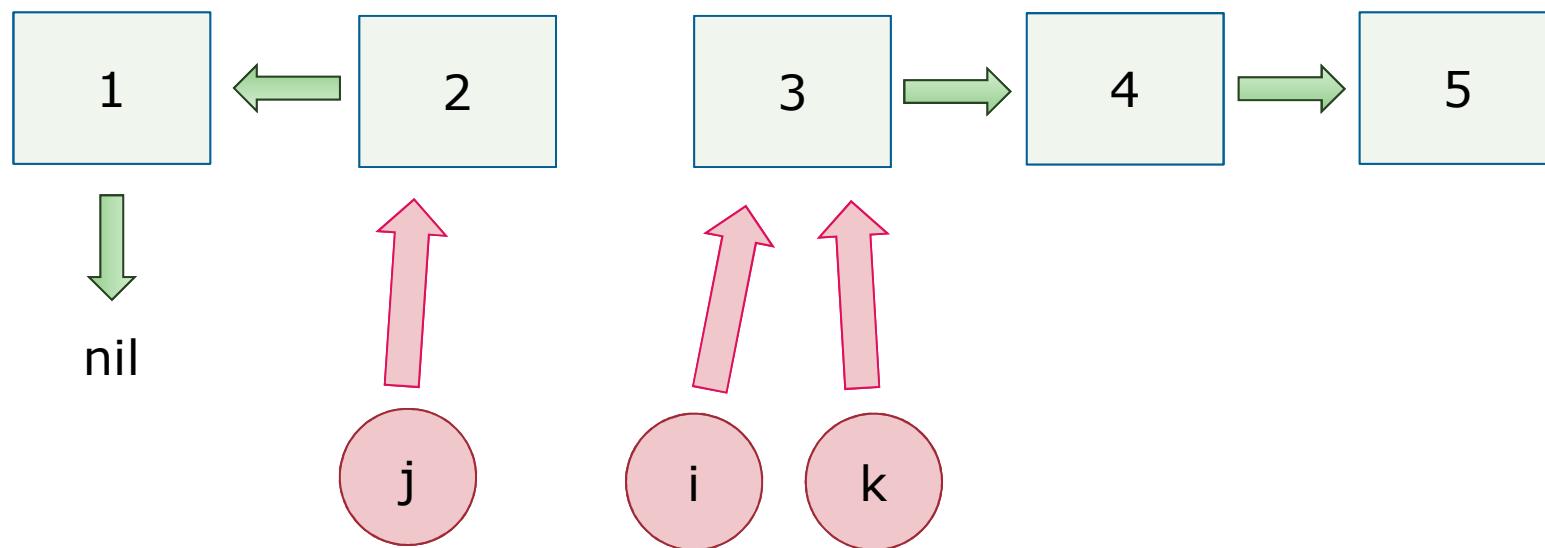
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Abstract List Reversal

```
while s is not empty do
    r' = head of s joined to r
    s' = tail of s
end while
```

Postcondition: $r' = \text{rev}(s)$

Separation

- In the abstract specification, r and s are assumed to be distinct.
- In normal data reification, the separation is preserved.

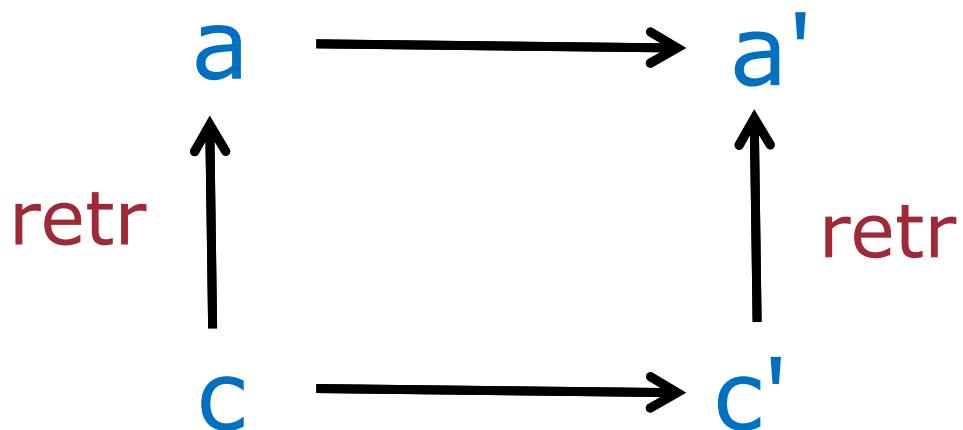
Separation

- In the abstract specification, r and s are assumed to be distinct.
- In normal data reification, the separation is preserved.
- For Reynolds's algorithm, we are reifying r and s onto parts of the same vector.
- This leads to a new form of reification: preservation of separation.

Implementation

The separation has to be stated as a predicate in the invariant.

The implementation can be shown to satisfy the abstract specification.



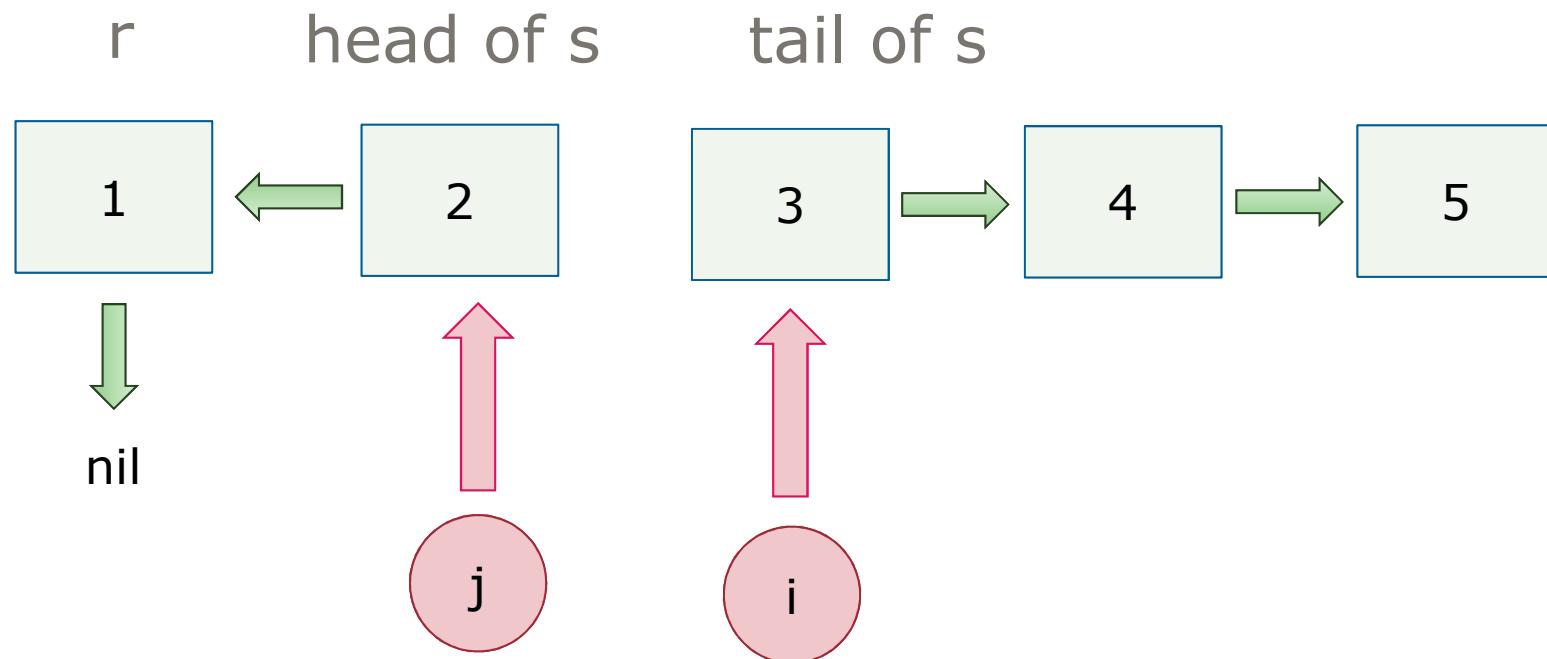
Proof – retr

$$\text{retr} : \Sigma_r \rightarrow \Sigma_a$$
$$\text{retr}(\text{mk-}\Sigma_r(m, i, j)) \triangleq \text{mk-}\Sigma_a(\text{gather}(i, m), \text{gather}(j, m))$$
$$\text{gather}(n, m) \triangleq$$

if $n = \text{nil}$
then []
else let $(v, p) = m(n)$ **in**
 $[v] \curvearrowright \text{gather}(p, m)$

Proof

At each step, recall: $r' = \text{head of } s \text{ joined to } r$;
 $s' = \text{tail of } s$



Concurrent DOM Trees

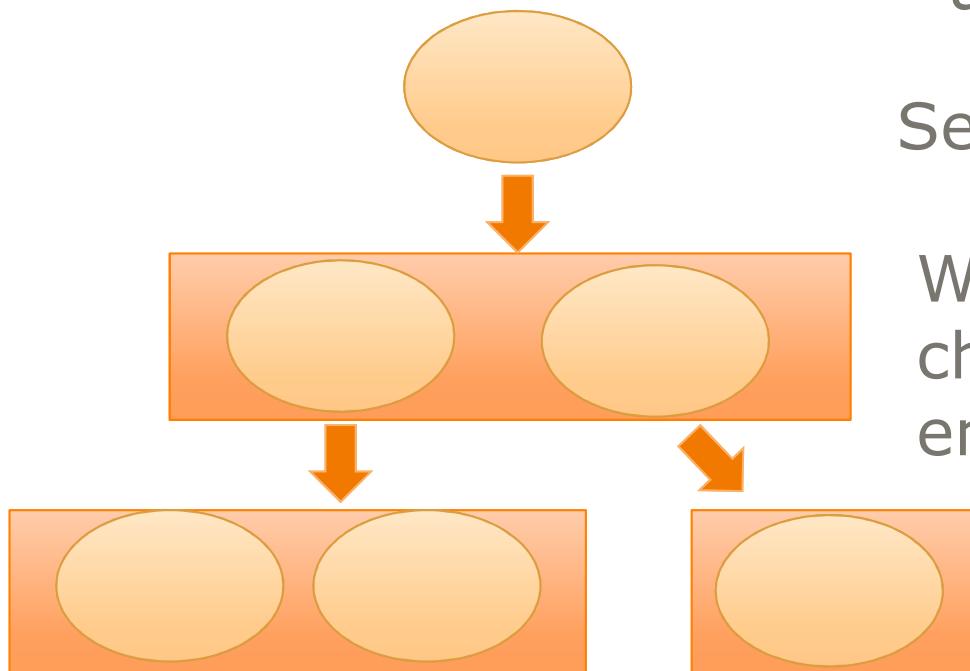
- Philippa Gardner & colleagues published proofs using separation logic of sequential algorithms for updating DOM trees.

Concurrent DOM Trees

- Philippa Gardner & colleagues published proofs using separation logic of sequential algorithms for updating DOM trees.
- Our first attempt at abstraction used recursive structures.
- This wasn't suitable as we needed NodeID's to match with DOM.

Concurrent DOM Trees

Abstract trees



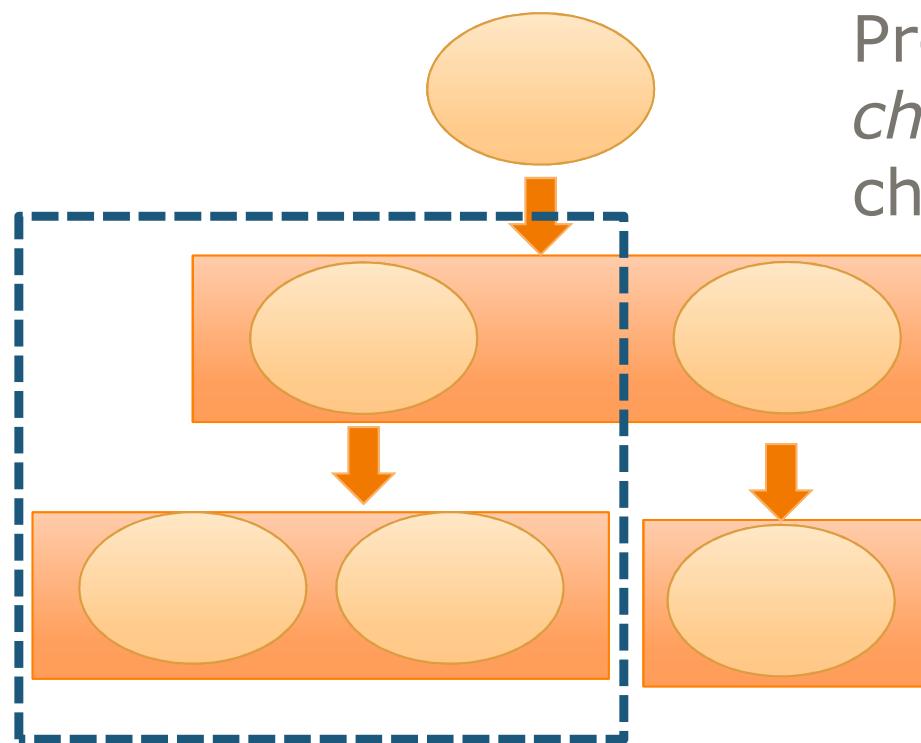
Each node has data and a list of children.

Separation is implied by:

Well-foundedness of the child to parent relation, ensuring no loops.

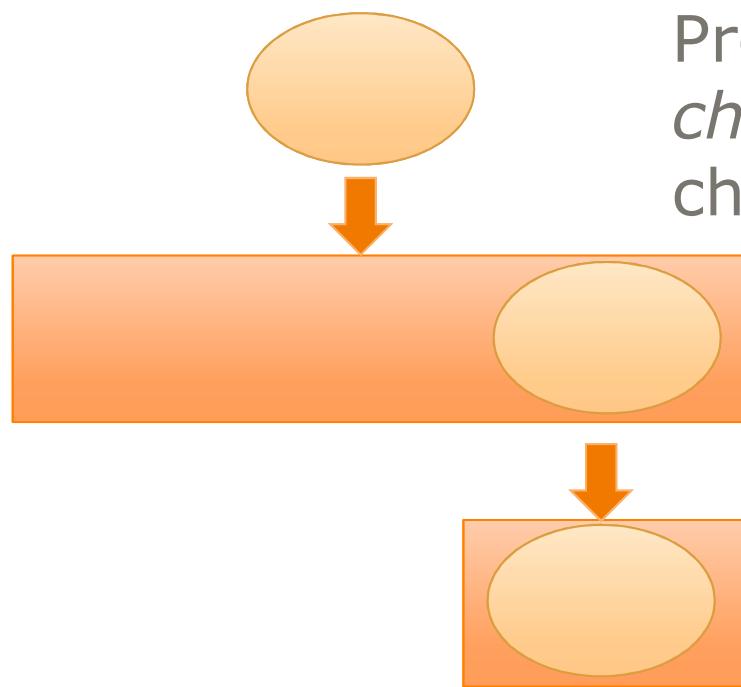
No child has more than one parent.

Abstract Sequential Remove



Pre: *parent* exists,
child is one of *parent*'s
children

Abstract Sequential Remove



Pre: *parent* exists,
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Post: The final state
is the same except for
that sub-tree
removed from its
parent.

From sequential to concurrent

- The sequential postcondition can state equalities about the whole system.

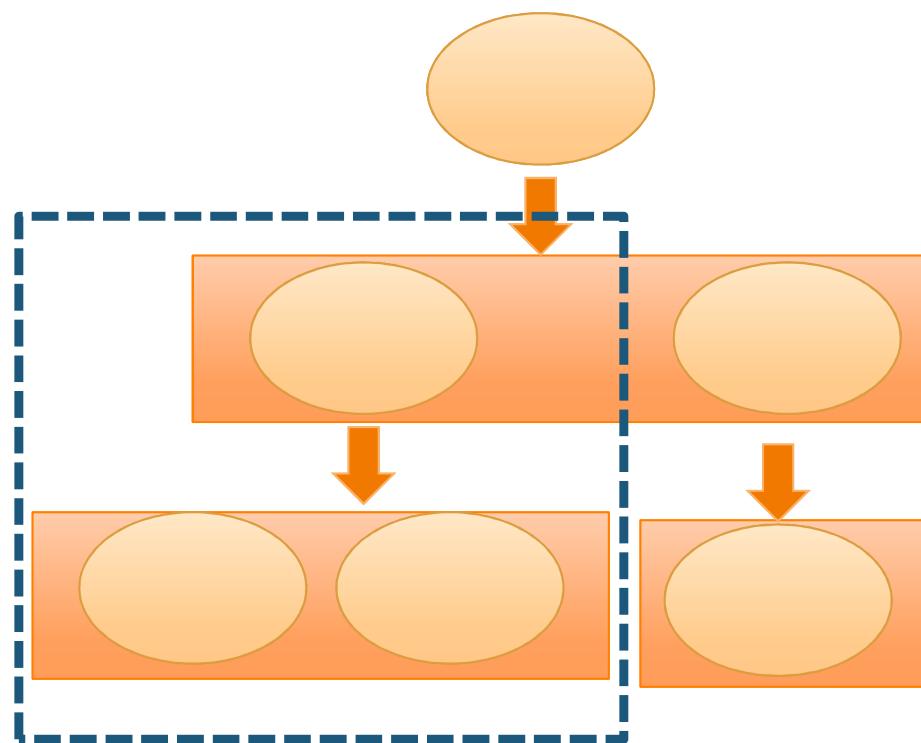
From sequential to concurrent

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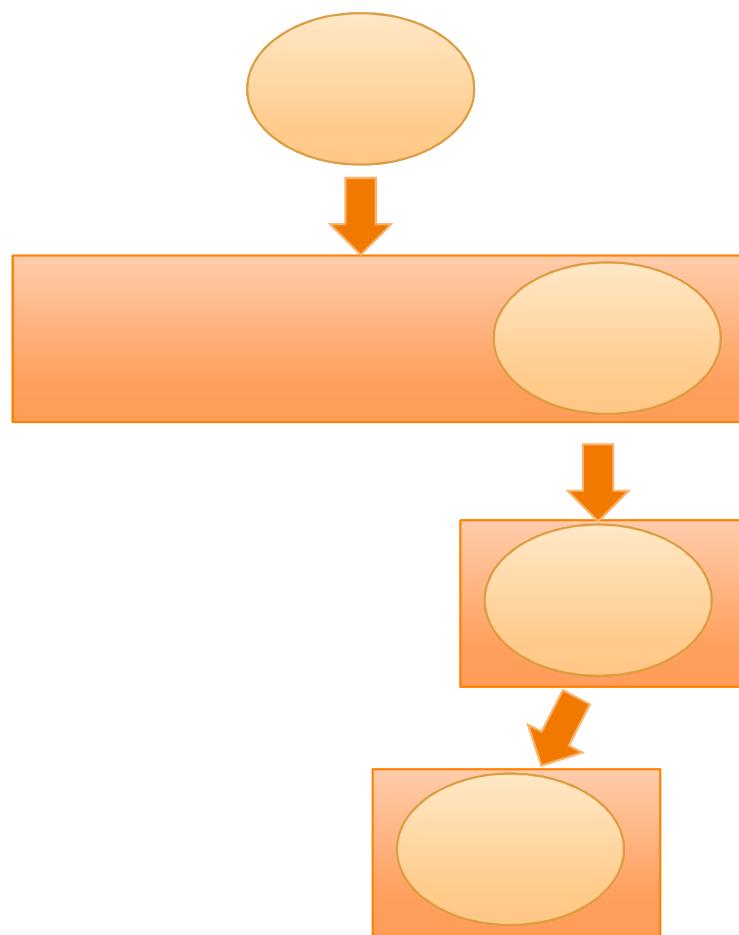
From sequential to concurrent

- The sequential postcondition can state equalities about the whole system.
- With concurrency, other processes may be operating simultaneously.
- The postcondition is weakened to form the concurrent postcondition and the guar.

Abstract Concurrent Remove

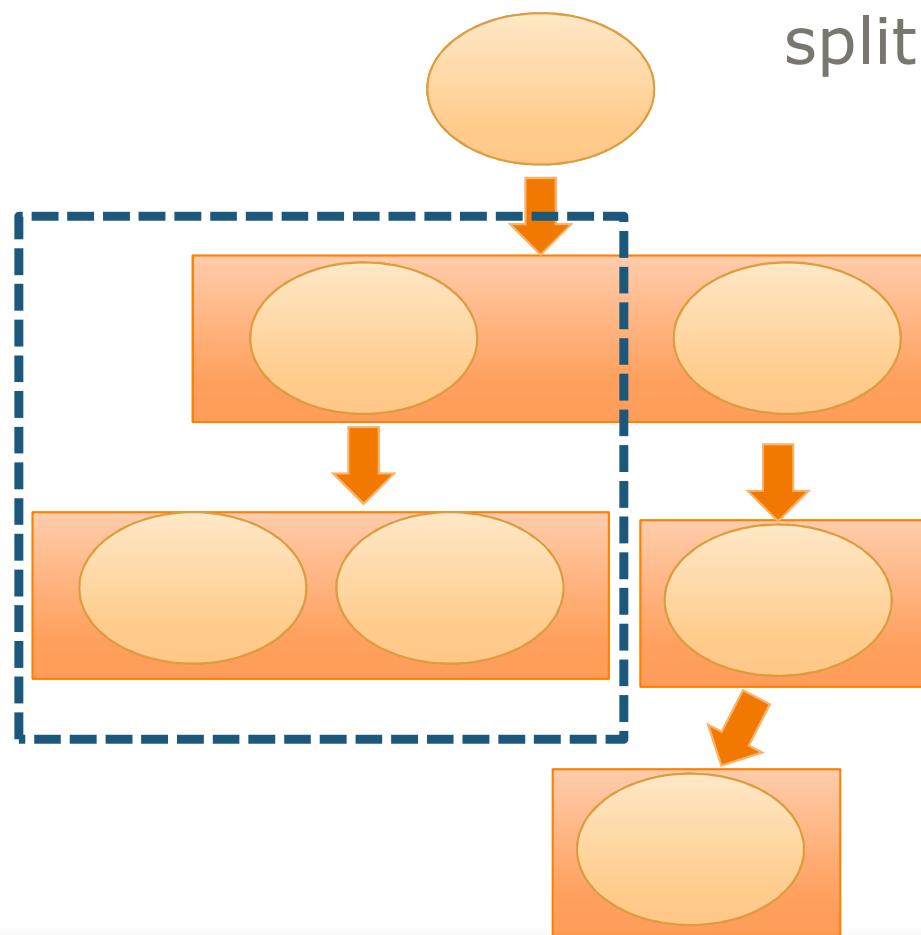


Abstract Concurrent Remove

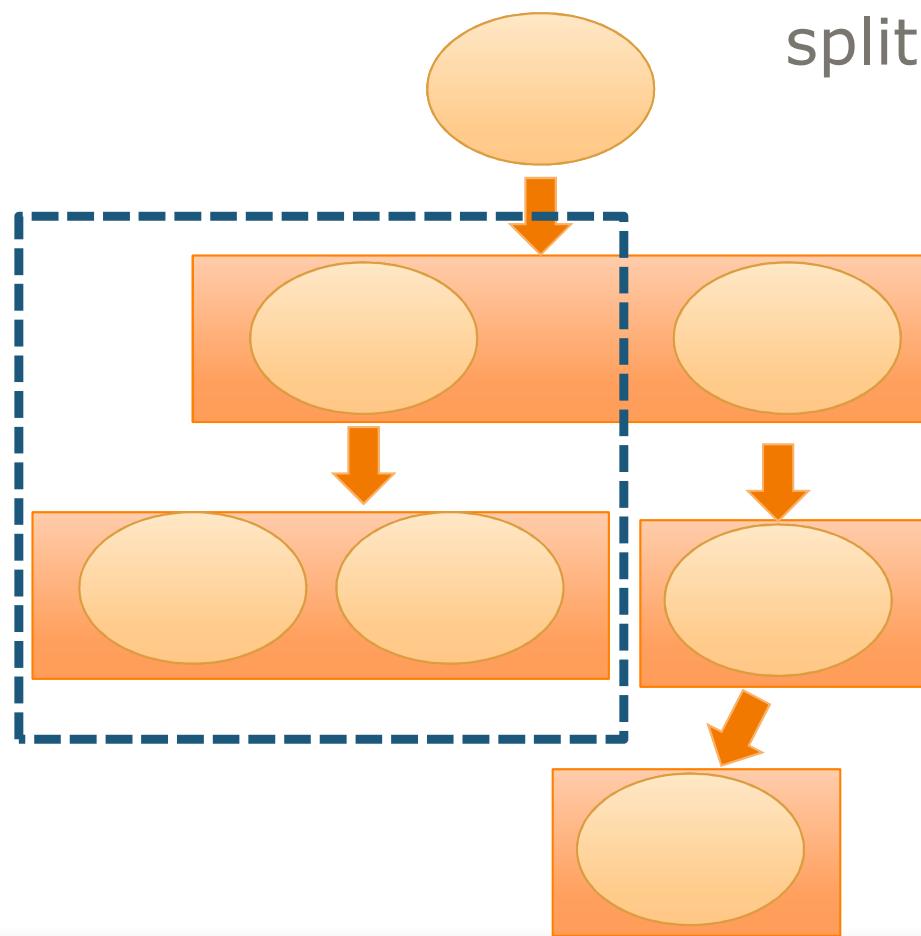


Abstract Concurrent Remove

The abstract post is now split into the post and guar:



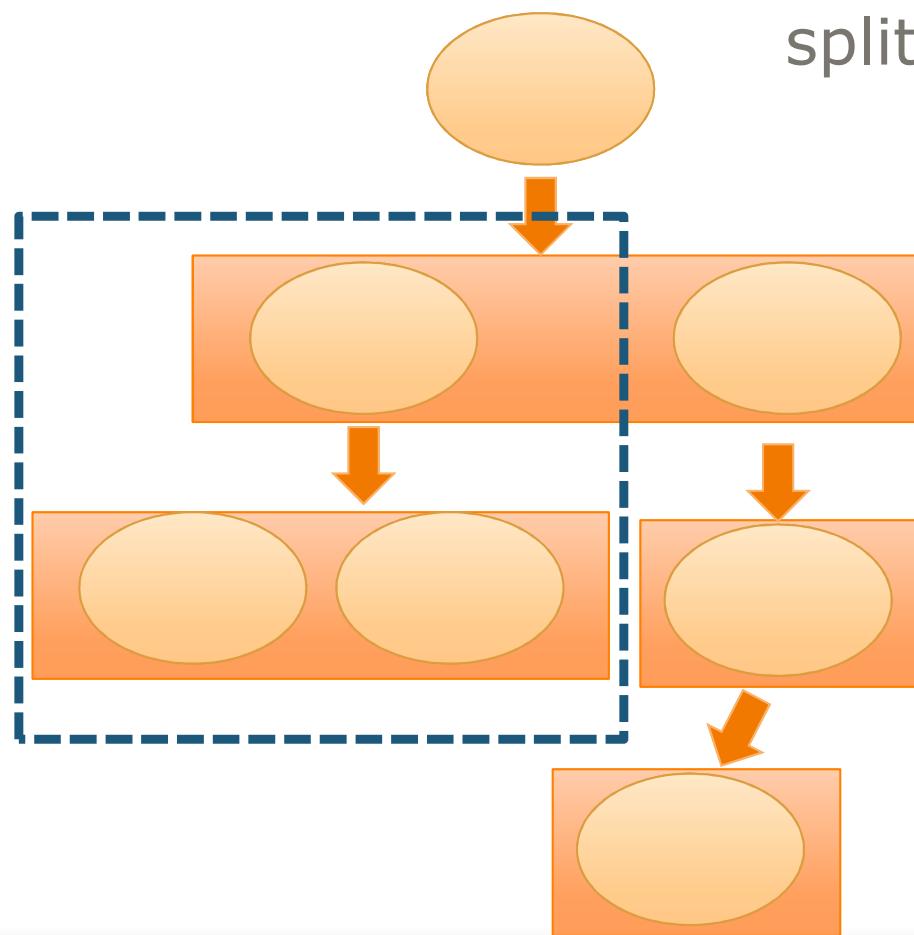
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post: *child* is removed from *parent's* children list. (Nothing about the rest of the tree).

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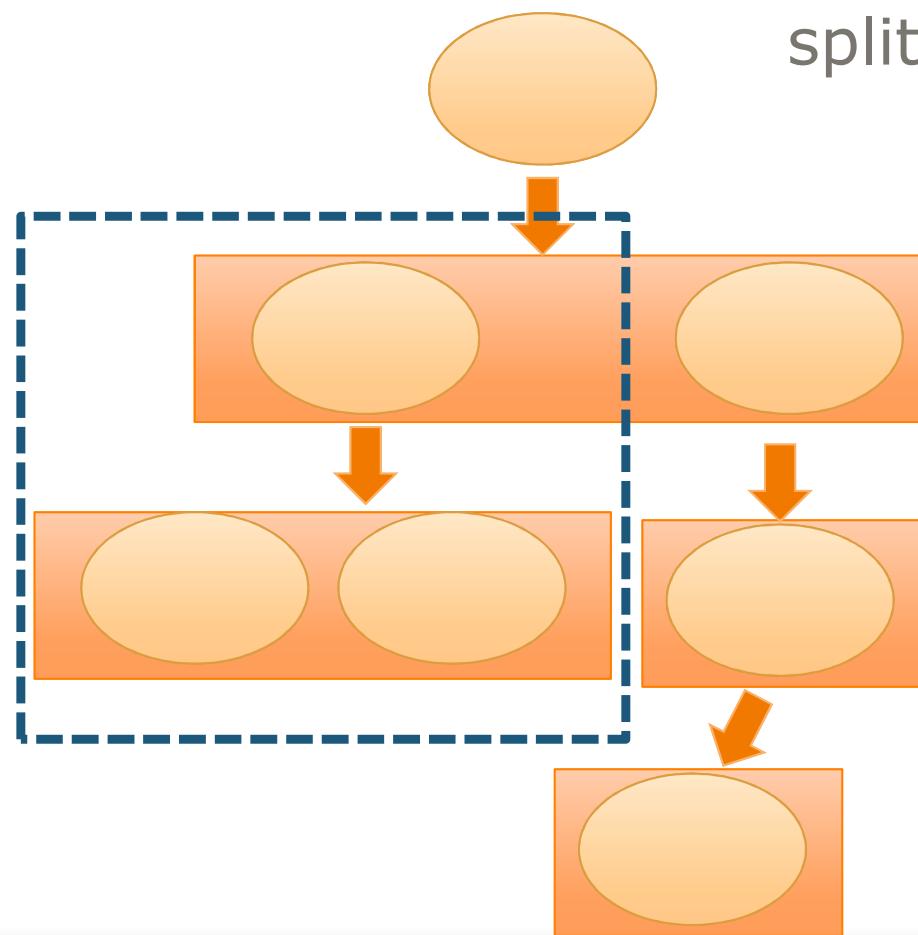


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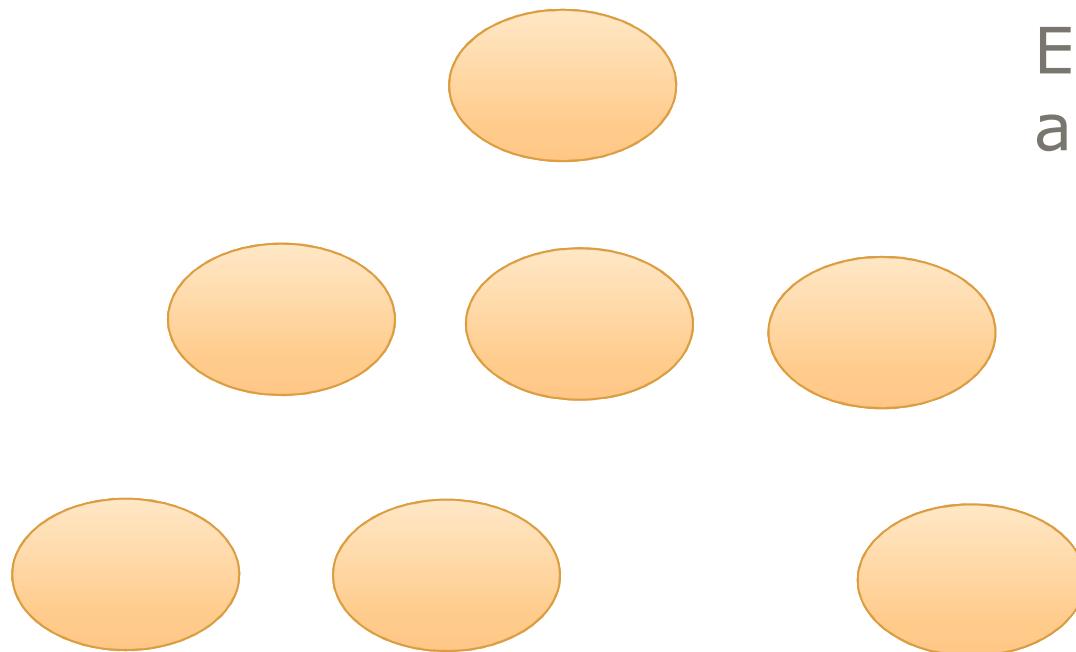
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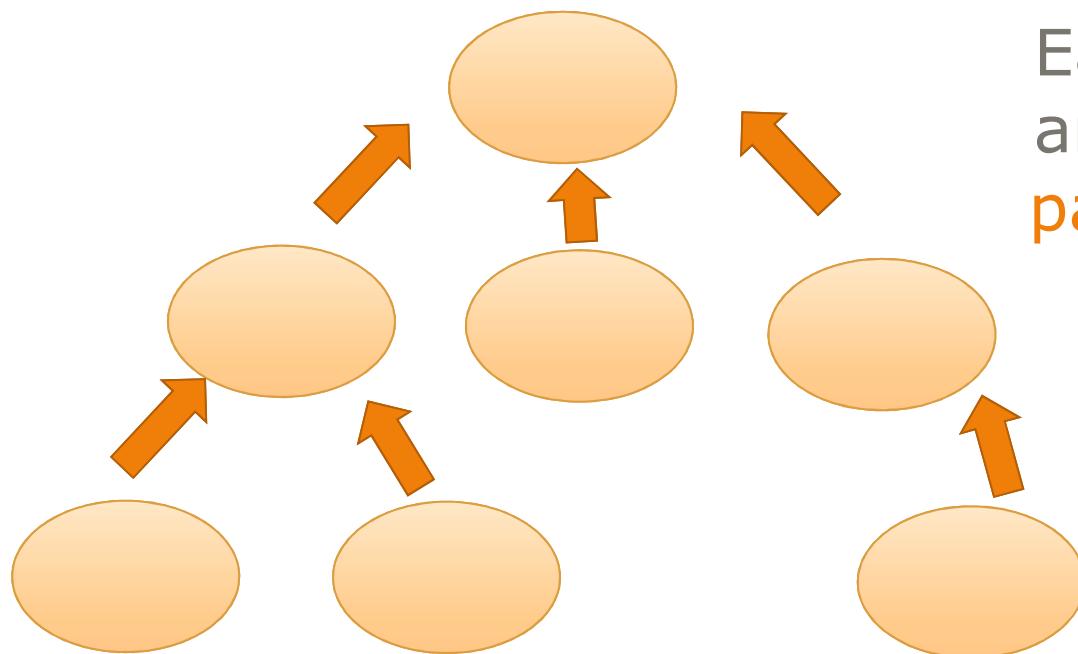
rely: *parent's* children won't change

Data Reification



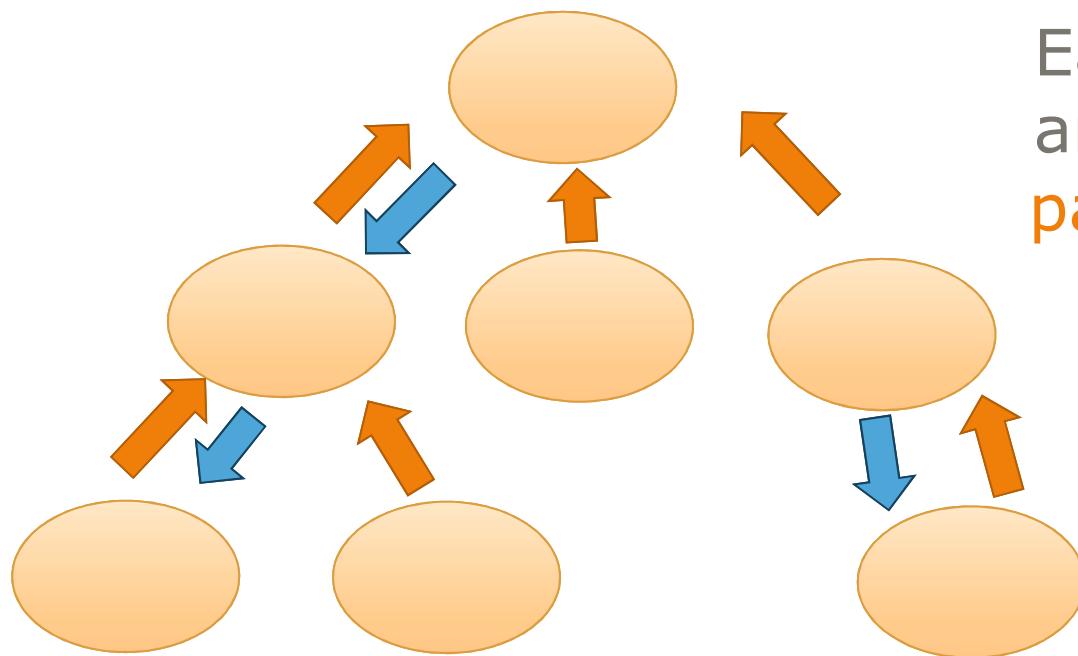
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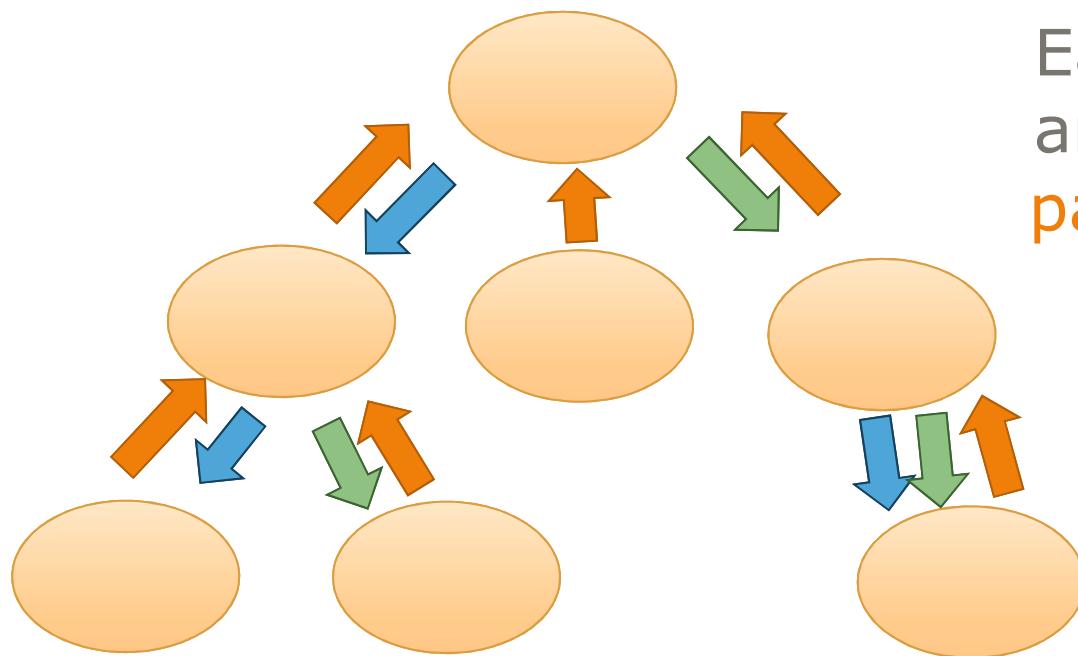
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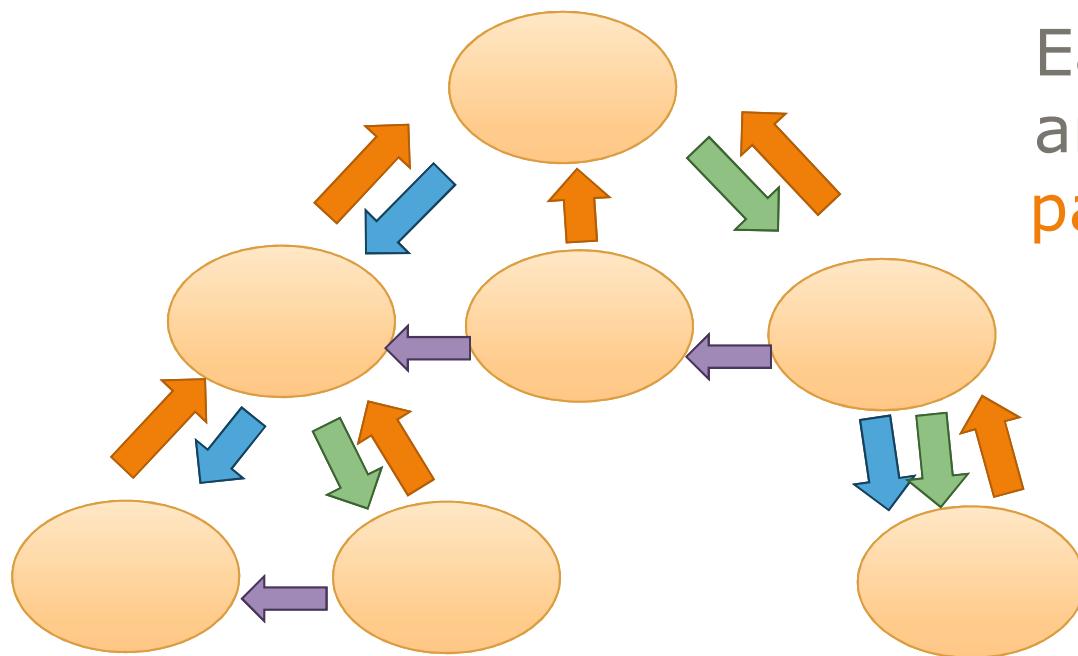
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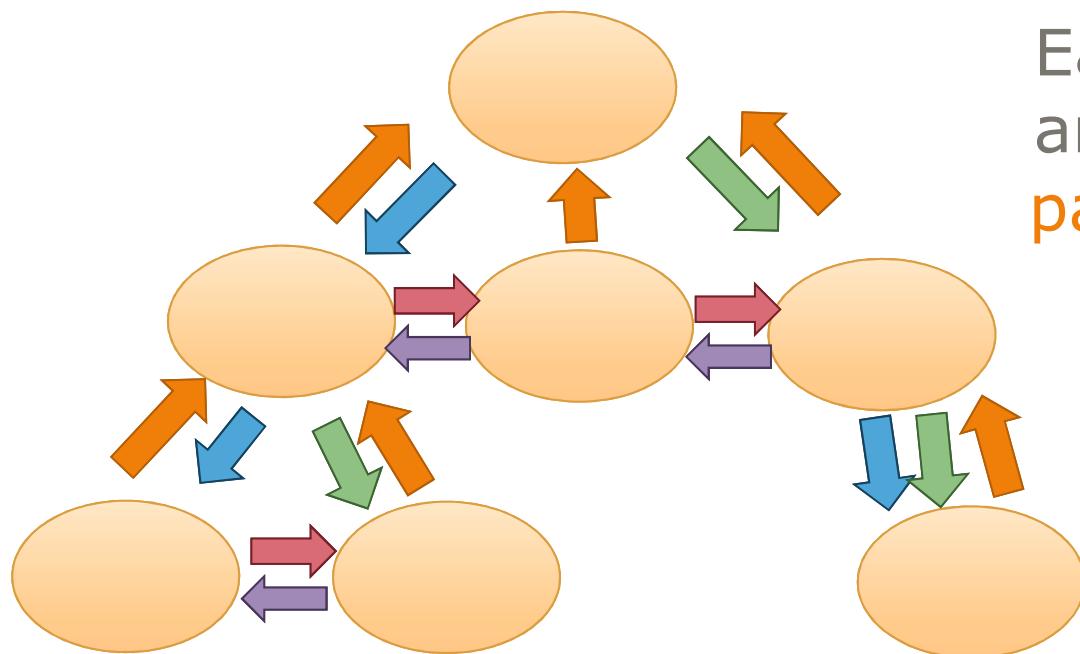
Each node has data and pointers to its **parent**, **first child**, **last child**,

Data Reification



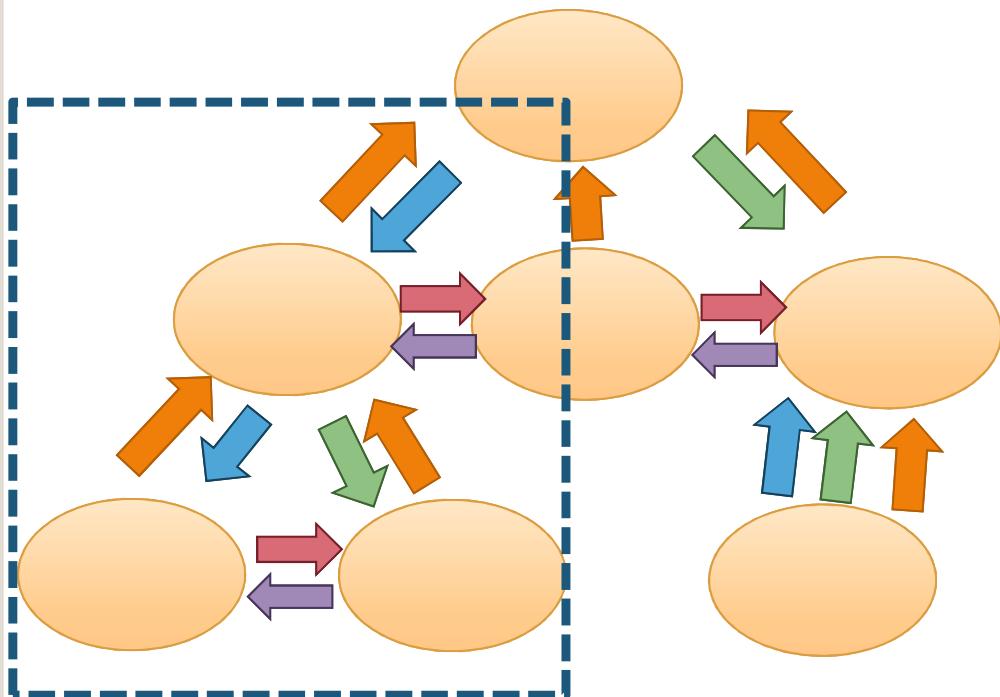
Each node has data and pointers to its **parent**, **first child**, **last child**, **previous sibling**

Data Reification



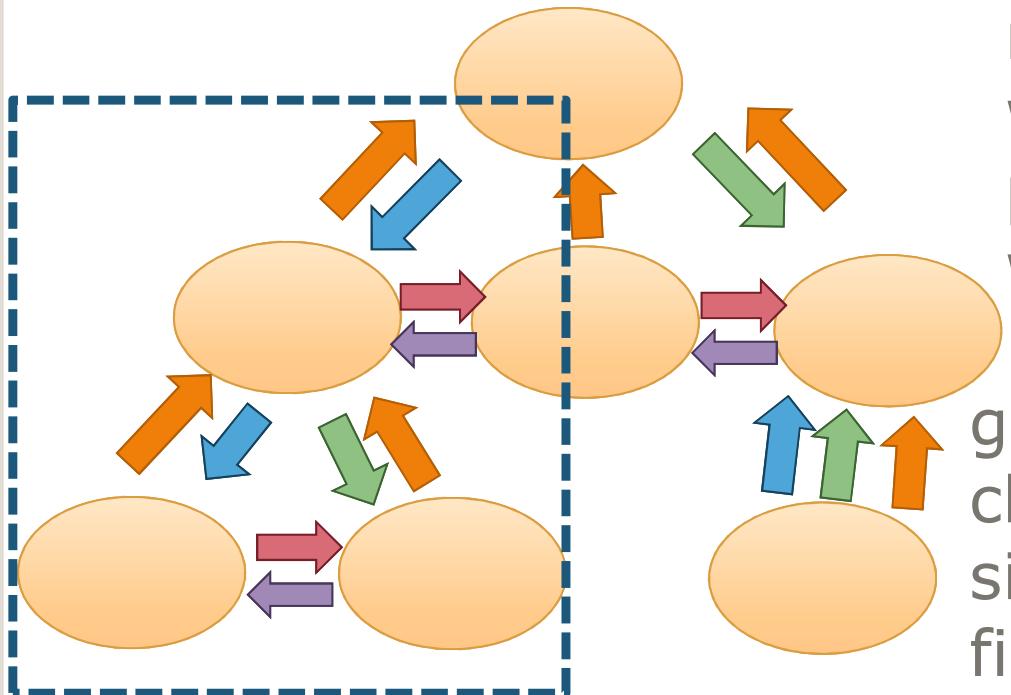
Each node has data and pointers to its **parent**, **first child**, **last child**, **previous sibling** and **next sibling**.

Reified Concurrent Remove



rely: *parent's children won't change, child's parent & siblings won't change.*

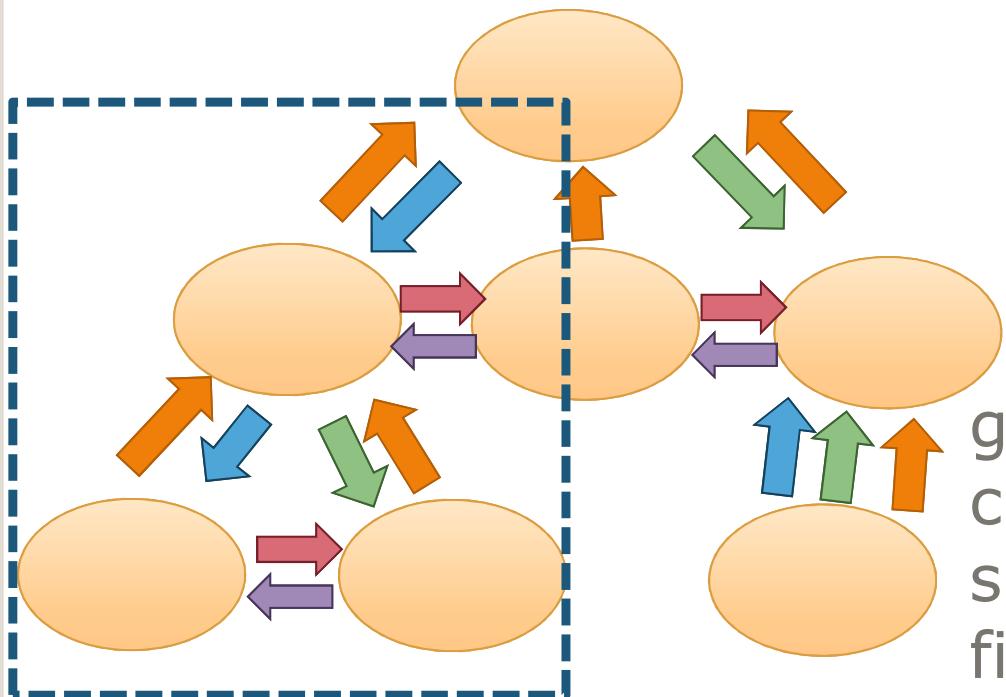
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Reified Concurrent Remove

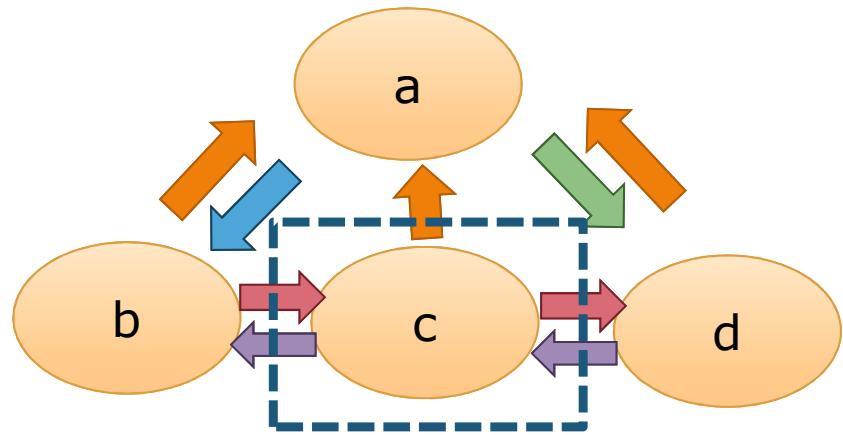


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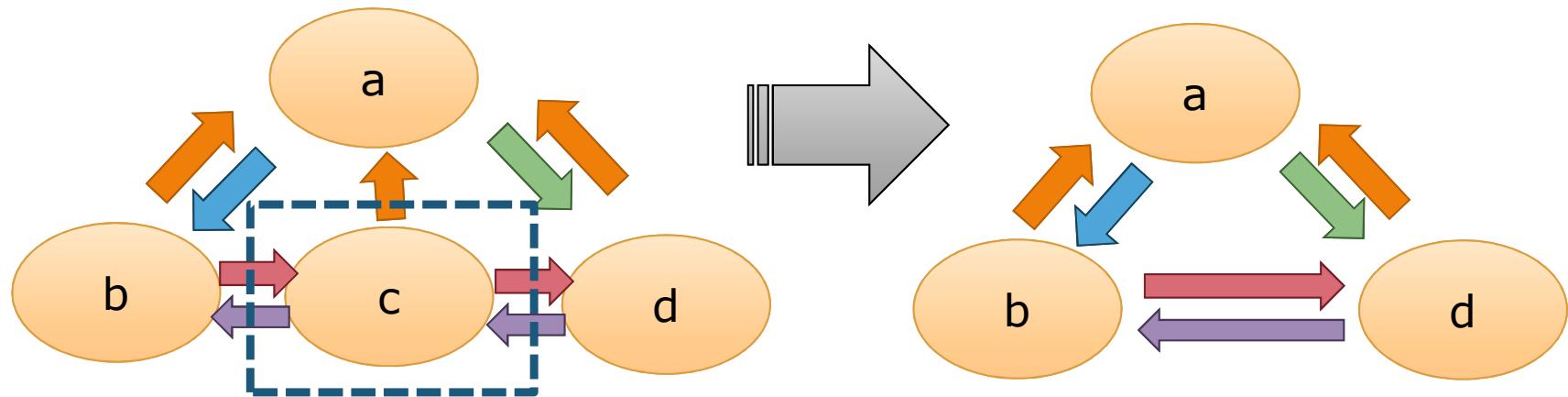
guar: This may only change *child's parent & sibling pointers, parent's first/last child pointers.*

post: *child's parent, prev & next siblings are nil and the sibling pointers are updated.*

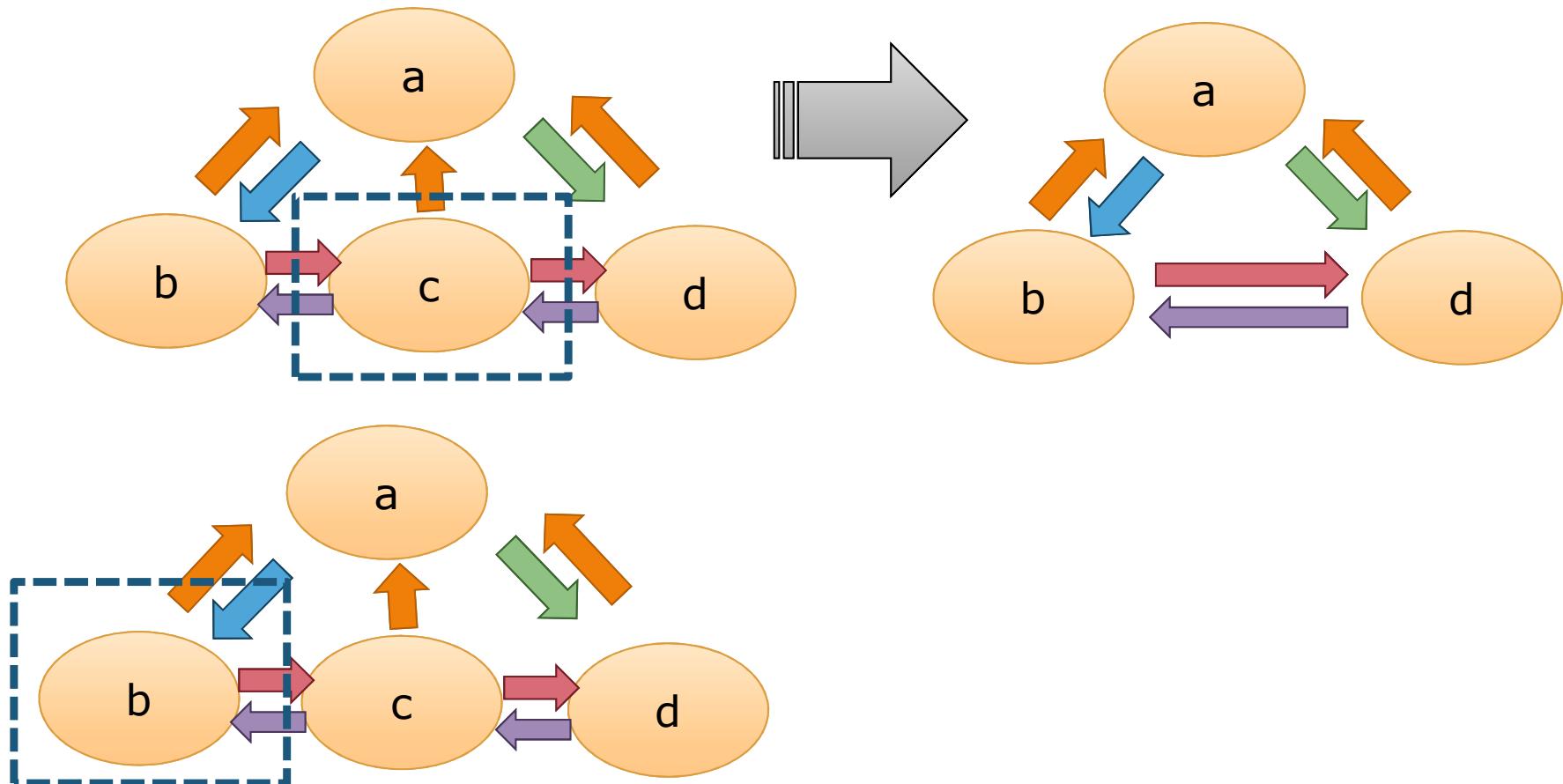
Updating siblings



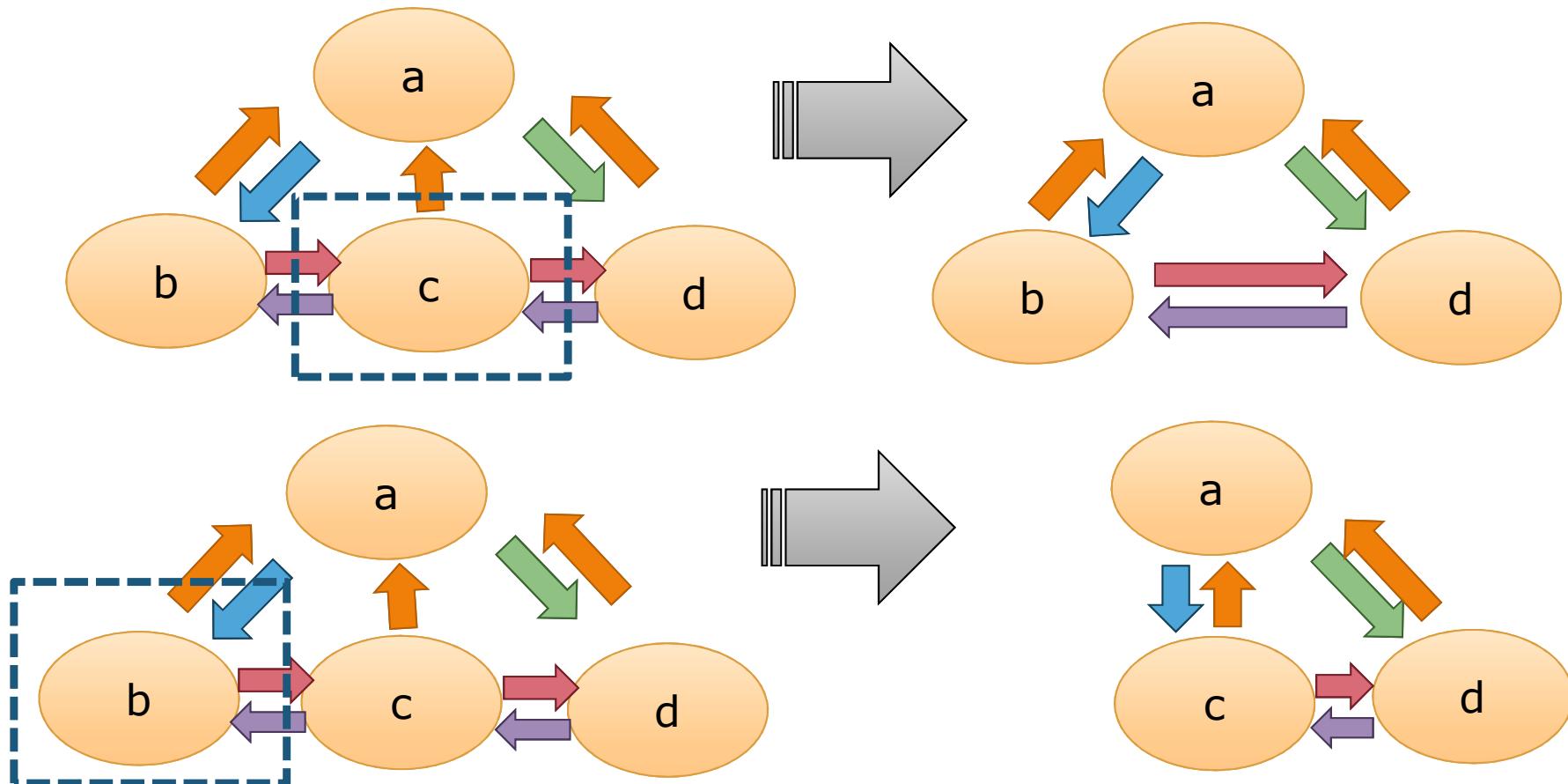
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- For this algorithm, the rely/guar conditions can be satisfied by locking the parent.
- Finer-grained locking can be accomplished by using special sentinel nodes at the corners.

Conclusions

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- Handling separation by reasoning with layers of abstraction seems promising.
- For concurrency, the sequential postcondition can be weakened to form the concurrent postcondition and the guar condition.
- The process was demonstrated from abstract sequential trees to abstract concurrent trees to reified concurrent trees.